

# Chapter 13

## Laser-Stimulated Fluorescence Refines Flight Modeling of the Early Cretaceous Bird *Sapeornis*

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### ABSTRACT

Unseen and difficult-to-see soft tissues of fossil birds revealed by laser-stimulated fluorescence (LSF) shed light on their functional morphology. Here we study a well-preserved specimen of the early pygostylian *Sapeornis chaoyangensis* under LSF and use the newly observed soft-tissue data to refine previous modeling of its aerial performance and to test its proposed thermal soaring capabilities. Under LSF, the body's lateral outline is observed, permitting direct estimates of the body's disc surface that generates drag during flight ( $S_b$ ). This surface and the body drag coefficient—which is better estimated knowing  $S_b$ —are influential parameters in modeling flight dynamics. In particular, we focus on two aspects of flight dynamics: the calculation of the power margin during flapping flight (power curve), and the sinking speed during gliding (glide polar). Results from revised models using our direct soft-tissue measurements support the notion that *Sapeornis* was a thermal soarer that glided for long periods. LSF also confirms the absence of a true alula in *Sapeornis*. While the deployment of the alular digit could have enhanced control during slow flight, the position of this digit along the handwing (distal part of the wing) suggests limited maneuverability. This study demonstrates how soft-tissue preservation can be incorporated into modeling of flight dynamics in light of ever-improving palaeontological imaging techniques.

### INTRODUCTION

Laser-stimulated fluorescence (LSF) uses high flux laser light to fluoresce fossil specimens at macro- and microscopic scales, improving imaging results with respect to conventional UV light (Kaye et al., 2015). LSF has revealed otherwise obscure and invisible osteological and soft-tissue details in fossil specimens facilitating the reconstruction of a range of paleobiological aspects (Kaye et al., 2015, 2019a;

2019b; Falk et al., 2016a; Mayr et al., 2016; Vinther et al., 2016; Wang et al., 2017; Yang et al., 2018). LSF has helped improve our understanding of theropod flight evolution by directly revealing soft-tissue outlines of the wings and body, providing invaluable insights into the functional morphology of the first flyers including potential candidates (e.g., the early-diverging paravian *Anchiornis* (Wang et al., 2017) and the early pygostylian *Confuciusornis* (Falk et al., 2016b).

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The flight dynamics of the Early Cretaceous early pygostylian *Sapeornis chaoyangensis* have been explored through quantitative approaches (Serrano and Chiappe, 2017). Morphofunctional evidence and aerodynamic models generated for this early bird indicated that *Sapeornis* flew by gliding over long periods and using ascending air currents in continental environments for soaring (i.e., thermal soaring). Serrano and Chiappe (2017) applied information from exquisitely preserved wing feathers to reconstruct the shape and size of the wings of this bird. Nonetheless, this approach was unable to include information from the body outline due to the absence of reliable nonfeather soft-tissue evidence from the studied specimens.

The body outline provides information about the body (= parasite) drag—the aerodynamic force generated by the body against the air stream—acting on a flying bird. As the generation of aerodynamic theoretical models is limited by a few parameters that are difficult to measure in flying birds (Pennycuick, 1969; Tucker, 1973; Rayner, 1999; Pennycuick, 2008), calculations for extinct birds require assumptions about such parameters (Burgers and Chiappe, 1999; Templin, 2000; Chatterjee and Templin, 2003; Ksepka, 2014; Serrano and Chiappe, 2017; Serrano et al., 2018). Among them, the body drag is particularly controversial and yet, it is proven to have a strong influence on the results of the models (Hedenström and Rosén, 2003; Taylor et al., 2016). LSF imaging of *Sapeornis* specimen STM 15-15 (Shandong Tianyu Museum of Nature, Pingyi, China) now provides information on body shape for the first time (fig. 1). Using this new soft-tissue information, we reanalyze the flight dynamics of this early pygostylian. We also provide a novel comparative analysis for the alular digit position of this bird, as this structure is very important for controlling flight at low speeds (Meseguer et al., 2012; Lee et al., 2015). Our refined results of the flight performance of this bird—incorporating both body drag and the role of the alular digit—allow us to test existing hypotheses about the

flying habits and paleoecological inferences of *Sapeornis*.

## MATERIAL AND METHODS

### FOSSIL AND ESTIMATIONS

*Sapeornis chaoyangensis* STM 15-15 (fig. 1) was examined and photographed at the Shandong Tianyu Museum of Nature (Pingyi, China). Bone measurements (table 1) were taken from photographs using ImageJ 1.51j8 (available from <http://imagej.nih.gov/ij>). Body width ( $L_b$ ) was measured from the LSF image as the maximum length from the dorsal margin of the vertebral column to the ventral contour of the feathered body (fig. 2). Despite the well-preserved feathers revealed by LSF, the wingtip (i.e., the distance between the distal end of the second phalanx of the major digit and the tip of the wing) and the wing chord (i.e., the distance from leading to trailing edge at wrist level) are not measurable for STM 15-15. Their values were obtained assuming an isometric variation for the skeletal wing (i.e., the added length of humerus, ulna, carpometacarpus, and major digit) of specimen DNHM 3078 (Gao et al., 2012). Following Serrano and Chiappe's (2017) study of the aerodynamics of *Sapeornis*, we estimated the body mass ( $M_b$ ), wingspan ( $B$ ), and lift surface ( $S_L$ ) of STM 15-15 using multiple regressions derived from a dataset of modern flying birds (Serrano et al., 2015; Serrano et al., 2017).

### LASER-STIMULATED FLUORESCENCE (LSF)

LSF images were collected using a refined version of the original protocol of Kaye et al. (2015) (Wang et al., 2017; Kaye et al. 2019a, 2019b). *Sapeornis* specimen STM 15-15 was imaged at the Shandong Tianyu Museum of Nature with a 405 nm violet laser. An appropriate long-pass blocking filter was used in front of a Nikon D810 DLSR camera lens to prevent image saturation by the laser. The laser was dispersed into a vertical line by a Laserline Optics



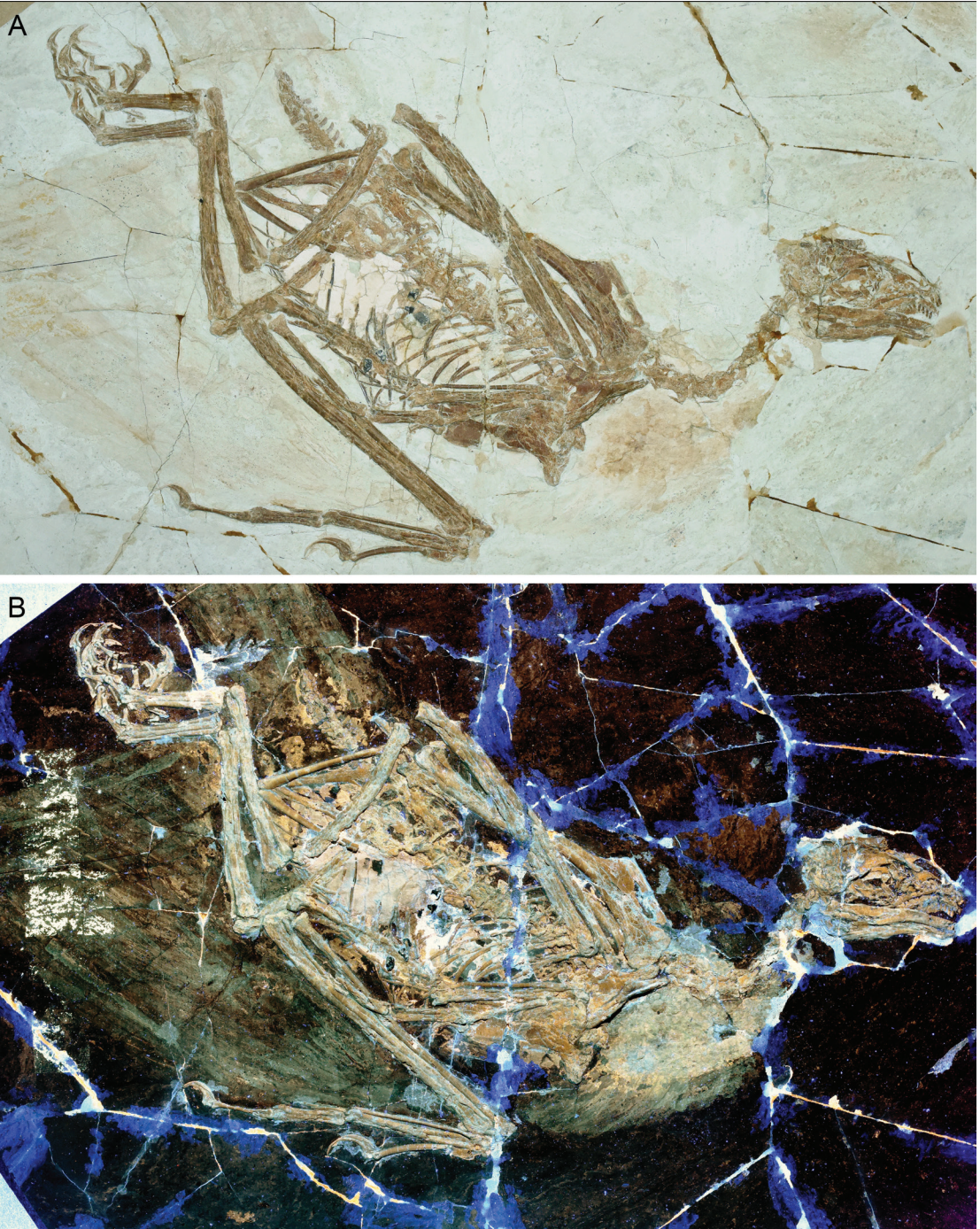


FIG. 1 Early pygostylian *Sapeornis* STM 15-15 shows faint soft-tissue details that **A**, under white light are vivid and **B**, under LSF, extensive.



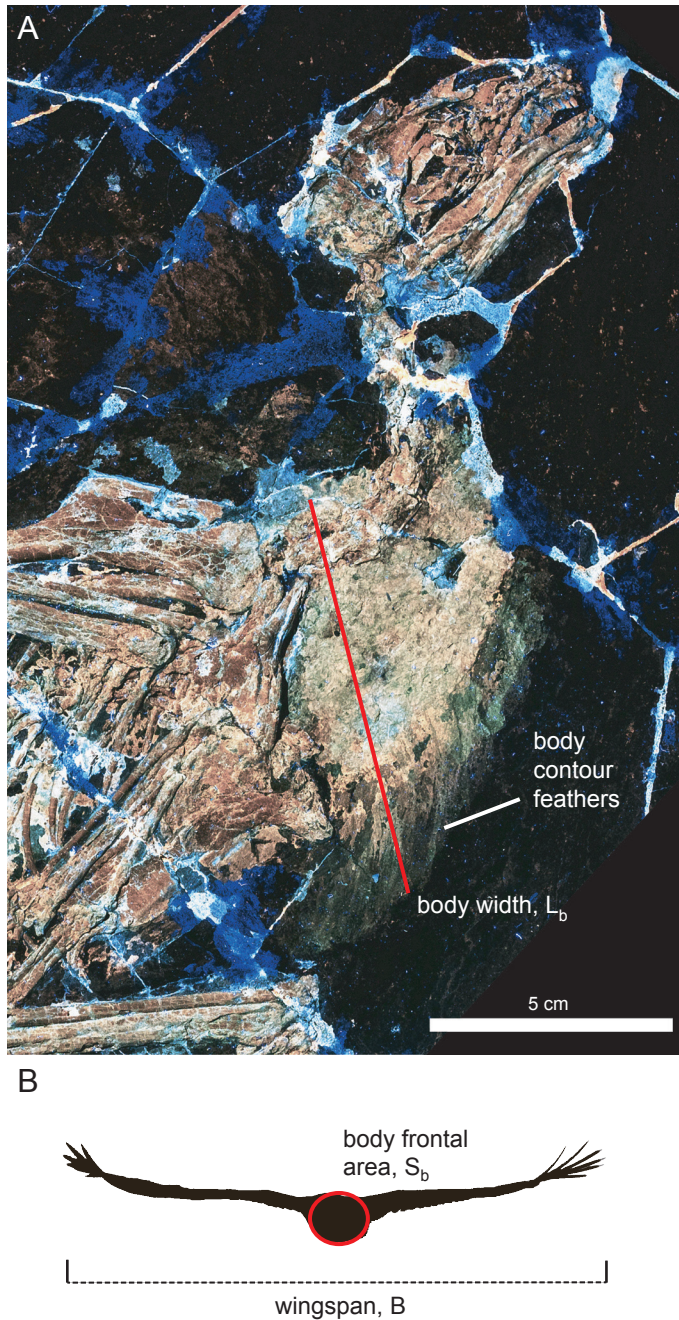


FIG. 2. **A.** The anterior region of *Sapeornis* STM 15-15 under LSF, showing contour feathers. **B.** Frontal view silhouette showing  $S_b$  and  $B$ .



Canada lens, which was mechanically swept repeatedly over the specimen during photo time exposures in the museum’s dark room. The images were postprocessed in Photoshop CS6 for sharpness, color balance, and saturation. Details of the theory behind LSF imaging can be found in Wang et al. (2017).

FLIGHT DYNAMICS MODELING

In modern birds, the maximum available power output (aerobic metabolism) for attaining active flight ( $P_{av}$ ) scales negatively with body size (Templin, 2000; Pennycuick, 2008).  $P_{av}$  was calculated using an oxygen consumption rate ( $V_{O_2}$ , mL/s) in which 1 mL  $O_2$ /s generates 20.1 W during aerobic activity (Schmidt-Nielsen, 1997). Values of  $V_{O_2}$  were estimated for *Sapeornis* using Equation 1, which was derived from birds flying at modern  $O_2$  concentration (i.e., 20.9 mL  $O_2$ /100 mL air; Bishop and Butler, 2015):

(1)  $V_{O_2} = 160 M_b^{0.74}$

By assuming a conversion efficiency of 0.2 from the total metabolic power input to  $P_{av}$  (Tucker, 1973; 1975; Pennycuick, 2008), and translating minutes into seconds—as Equation 1 was derived from  $V_{O_2}$  measured in mL/min—the  $P_{av}$  at modern conditions was calculated using Equation 2:

(2)  $P_{av} = 20.1 \times 0.2 / 60 V_{O_2}$   
 $P_{av} = 0.067 V_{O_2}$

Values of  $P_{av}$  for STM 15-15 were adjusted to the  $O_2$  atmospheric levels at 120 Myr, the estimated time of deposition for the fossil (Ward and Berner, 2011), through the percentage of variation between concentrations today and in the past (Serrano et al., 2019), calculated using Equation 3 (where AOC is atmospheric  $O_2$  concentration):

(3)  $P_{av} = (0.067 V_{O_2} \cdot \% \Delta AOC) + 0.067 V_{O_2}$

TABLE 1  
Anatomical measurements (in mm) of *Sapeornis* STM 15-15

Asterisk indicates estimated measurements due to specimen damage or incomplete preservation.

Element	Measurement
Humerus	132.7
Humerus midshaft width	6.9
Distal humeral width	14.2
Deltpectoral crest	48
Bicipital crest	15.6
Ulna	129.5
Ulna midshaft width	7.0
Distal ulnar width	9.1
Radius	128.2
Radius midshaft width	3.5
Carpometacarpal length (semilunate to major metacarpal)	61.7
Alular digit position (semilunate to distal end of alular mc)	16.7
Proximal carpometacarpus width	11.1
Metacarpus midshaft width	6.5
Major metacarpal midshaft width	4.3
Alular digit	31.5
Major digit-1	30
Major digit-2	26.4
Wing tip*	225.8
Wing chord*	240.7
Femur	68.4
Femur midshaft width	5.9
Tibiotarsus	79.6
Metatarsal	43.6
Body width	95.7

For a given bird flying, the power curve that relates its forward speed ( $V_f$ ) with its mechanical power output necessary for flapping flight ( $P_{mec}$ ) is U-shaped (Pennycuick, 1969; Tucker, 1973; Rayner, 1999). This theoretical relationship is mostly supported by direct measure of the input power in modern birds flapping (Bishop and Butler, 2015). We constructed power curves for

*Sapeornis* STM 15-15 using the software Flight v. 1.24 (www.bio.bristol.ac.uk/people/pennycuick.htm) (Pennycuick, 2008). The values of  $P_{mec}$  for a range of velocities  $V_t$  were calculated according to Equation 4, as the summation of the induced power ( $P_{ind}$ ; Equation 5, where  $k$  is the induced power factor and  $g$  is gravitational acceleration), the parasite power ( $P_{par}$ ; Equation 6, where  $S_b$  is the frontal area of the body,  $C_{Db}$  is the body-drag coefficient,  $\rho_{air}$  is the density of air and  $B$  is the wingspan), and the profile power ( $P_{pro}$ ; Equation 7, where  $V_{mp}$  is the minimum power speed and  $C_{pro}$  is the profile power constant).

- (4)  $P_{mec} = P_{ind} + P_{par} + P_{pro}$
- (5)  $P_{ind} = 2k [M_b g]^2 / V_t \pi B^2 \rho_{air}$
- (6)  $P_{par} = \rho_{air} V_t^3 S_b C_{Db} / 2$
- (7)  $P_{pro} = [2k (M_b g)^2 / V_{mp} \pi B^2 \rho_{air} + \rho_{air} V_{mp}^3 S_b C_{Db} / 2] C_{pro} / [B^2 / S_L]$

These calculations require assumptions for some components, particularly when applied to fossil taxa (Serrano et al., 2018). For example,  $k$ —a parameter that accounts for any deviations from elliptical distribution of the lift across the wingspan— was set at  $k = 1.2$ , a value typically observed in aircraft, while  $C_{pro}$  was fixed at 8.4 to make  $P_{pro}$  proportional to the wing area (Pennycuick, 2008). The body-drag components (i.e.,  $S_b$  and  $C_{Db}$ ) are highly influential parameters (Taylor et al., 2016), and they were addressed, as explained in the next section. The cruising speed or the speed with minimum cost of transport ( $V_{mr}$ ), was calculated as the speed where the tangent to the power curve intersects with the origin of the speed-power plot (Rayner, 1999).

The dynamics of gliding were studied through the glide polar graph that relates the sinking speeds ( $V_z$ ) to a range of forward speed ( $V_t$ ).  $V_z$  calculated with Equation 8, where  $D$  is the total aerodynamic drag resulting from the addition of the induced, parasite and profile drags (Pennycuick 2008). We also assumed that wingspan decreases as a linear function of speed (i.e., linear reduction command of Flight v. 1.24) and used an induced drag factor equal to 1.0 (Taylor et al., 2016):

$$(8) V_z = D V_t / M_b g$$

#### BODY-DRAG ESTIMATION

The body frontal area ( $S_b$ ) of STM 15-15 was calculated directly (Equation 9) from the measurement of the body width ( $L_b$ ; fig. 2). For comparison,  $S_b$  was also calculated from its allometric relationship with the body mass,  $M_b$  (Equation 10) (Pennycuick et al., 1988).

- (9)  $S_b = \pi * (L_b / 2)^2$
- (10)  $S_b = 0.00813 * M_b^{0.666}$

The body-drag coefficient ( $C_{Db}$ ) is a dimensionless value that indicates the streamlined degree of the body (Pennycuick, 2008).  $C_{Db}$  value is difficult to measure in modern birds, and we used different approaches for obtaining it in *Sapeornis*.

The first approach, named model 1, was based on the Reynold's number of the body ( $Re_b$ ) (Equation 11).  $C_{Db}$  was calculated from its negative allometry with  $Re_b$  (Equation 12) found in 39 modern passerines (Hedenström and Liechti, 2001).

- (11)  $Re_b = V_t L_b \rho_{air} \mu^{-1}$
- (12)  $C_{Db} = 0.70 - (5.8 \times 10^{-6}) Re_b$

We took the  $\rho_{air}$  at 120 Myr (i.e., 1.209 kgm<sup>-3</sup>; Serrano et al., 2019), while the dynamic viscosity of the air,  $\mu$ , was assumed at modern standard conditions (i.e., 1 atm, 20° C). Under this approach  $C_{Db}$  varies with  $Re_b$ , and this  $Re_b$  is dependent on  $V_t$ . We calculated  $Re_b$  and  $C_{Db}$  at each  $V_t$  from 7 to 24 ms<sup>-1</sup> (i.e., the range for plausible flight speed of *Sapeornis* given by Serrano and Chiappe 2017). The average value of these  $C_{Db}$  was used to construct the models.

Another approach, model 2, obtained  $C_{Db}$  from  $S_b$  (Eq. 10) and the equivalent flat-plate area ( $A$ ) (Equation 13). For estimating  $A$ , we followed the approach from Taylor and Thomas (2014) that assumes a body drag equivalent to the drag on a flat plate with 1% of the area of the wings (Equation 14). Rearranging equations 13 and 14,  $C_{Db}$  was estimated in Equation 15.



$$(13) A = S_b \times C_{Db}$$

$$(14) A = 0.01 S_L$$

$$(15) C_{Db} = (0.01 S_L) / S_b$$

Lastly, we generated models with minimum and maximum  $C_{Db}$  values (models 3 and 4, respectively) to obtain an uncertainty range for the curves. The minimum  $C_{Db}$  was fixed at 0.1, a value that assumes a well-streamlined body with no drag generated from the legs and feet (Pennycuik, 2008). We selected the maximum  $C_{Db}$  at 0.5 because Hedenström and Liechti (2001) suggested that  $C_{Db}$  experimentally measured above 0.4 would come from the underestimation of the maximum effort of the flying birds tested, although they found outliers above 0.5. Models 3 and 4 used  $S_b$  from Equation 10.

## RESULTS

For *Sapeornis* STM 15-15 we estimated a  $M_b$  of 0.927 kg, a  $B$  of 122.3 cm and  $S_L$  of 0.235 m<sup>2</sup>, within the range provided by Serrano and Chiappe (2017). From its  $M_b$ , STM 15-15 could generate a maximum  $P_{av}$  of 9.0 W.  $C_{Db}$  values calculated from  $Re_b$  (model 1:  $C_{Db} = 0.31$ ) and from  $A$  (model 2:  $C_{Db} = 0.30$ ) are within the range established between the minimum and maximum values (i.e., 0.1 and 0.5 in the models 3 and 4, respectively). The three power curves (models 1, 2, and 4) show that the  $P_{mec}$  required for sustaining flapping flight was above the value of  $P_{av}$  for the full range of  $V_t$  (fig. 3A). In model 3—the one assuming the minimum  $C_{Db}$ —the  $P_{mec}$  was slightly under  $P_{av}$  at starting values of the  $V_t$  range. At cruising speeds  $V_{mr}$ , all models show that  $P_{mec}$  was higher than the  $P_{av}$ . The four aerodynamic models thus indicate that STM 15-15 could not generate sufficient  $P_{mec}$  for sustaining a prolonged flight through wing flapping.

The glide polar graph illustrates that in STM 15-15 sinking took place at low forward speeds (fig. 3B). This gliding pattern, observed in the four analyzed models (1, 2, 3, and 4), has values within the range of modern birds that use thermal soaring. Model 1—the one using direct

information from the fossil's body outline—clearly shows a glide pattern like a thermal soarer; when STM-15-15 reached its maximum lift-to-drag ratio (11.8–12.1), its gliding-forward velocity was 9.7 ms<sup>-1</sup> (9.2–10.1 ms<sup>-1</sup>) and its sinking speed 0.82 ms<sup>-1</sup> (0.76–0.86 ms<sup>-1</sup>). These values are remarkably close to those for the Red-Tailed Hawk (*Buteo jamaicensis*), as reported in Serrano and Chiappe (2017: table 2).

The position of the alular digit in STM 15-15 (fig. 4)—here based on the location of the distal end of the alular metacarpal—is farther from the wrist than that observed in similar-sized soaring birds (fig. 5). Such a distalward position resembles modern birds that are poorly competent at unsteady maneuvers, typically divers (i.e., loons, grebes, auks, diving ducks, cormorants, and storm petrels) or occasional fliers (i.e., landfowls, waterfowls, and rails). Pelicans and South American screamers, more than double the size of STM 15-15, were the only thermal soarers with a comparable distalward position of the alular digit (fig. 5).

## DISCUSSION

Our study is the first to use the preserved body outline of a fossil bird—as revealed under LSF (fig. 2B)—to refine its flight modeling. Visualization of the body outline of STM 15-15 allows a direct measure of the body surface that generated drag during flight ( $L_b$  and  $S_b$ ) (i.e., model 1), whereas previous aerial models of *Sapeornis* (Serrano and Chiappe, 2017) assumed a modern allometric variation for  $S_b$  (Pennycuik et al., 1988) (i.e., models 2, 3 and 4). Visualization of the body outline also allows a direct calculation of the body-drag coefficient ( $C_{Db}$ ), which has proven especially controversial to calculate from theoretical approaches (Taylor et al., 2016). Our results show that  $C_{Db}$  value calculated in model 1—direct calculation through the Reynolds number of the body (Hedenström and Liechti, 2001)—was similar to the value calculated in model 2, a calculation that assumed a body-drag equivalent to the drag on a flat plate with 1% of

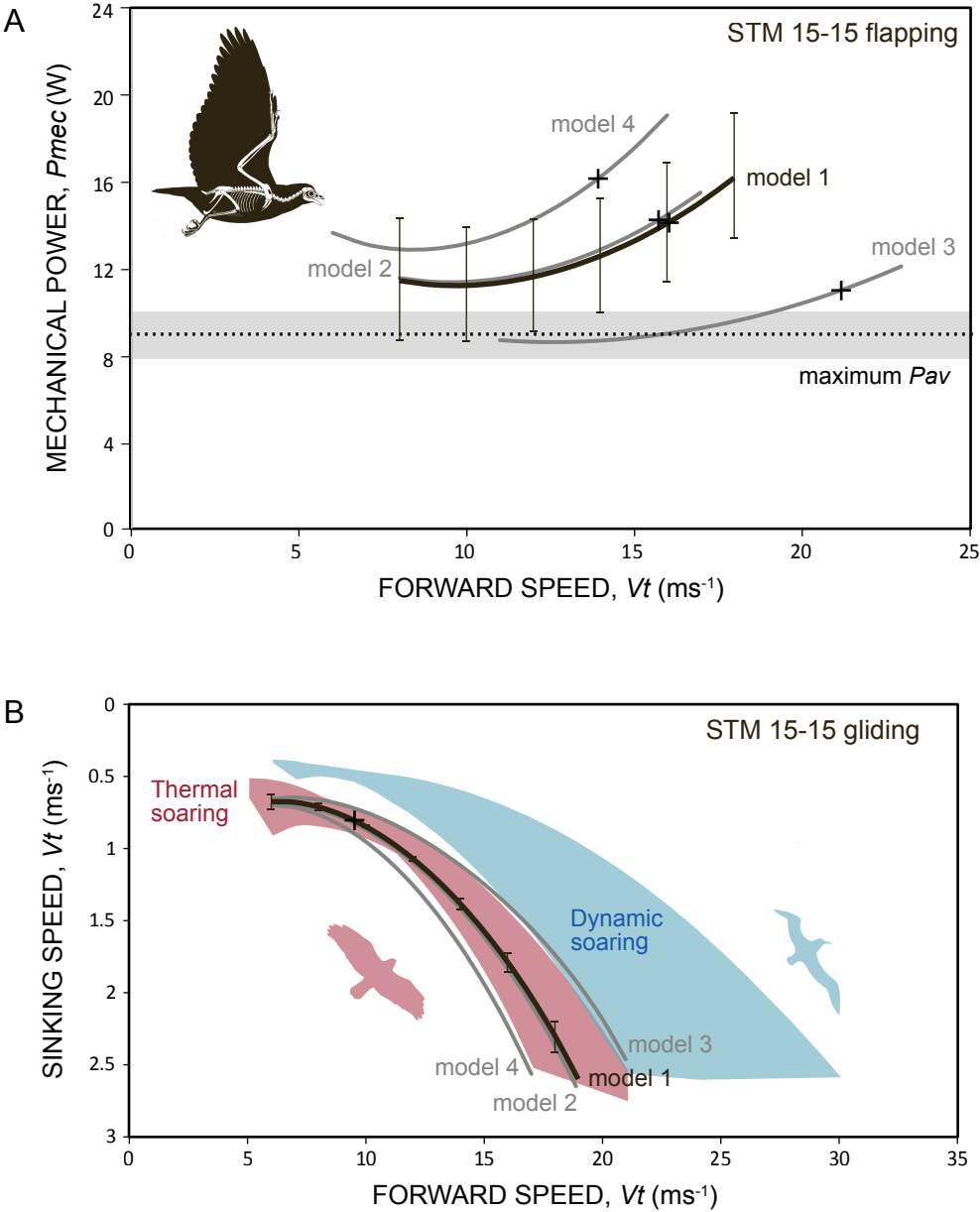


FIG. 3. **A.** Power margin in four models of *Sapeornis* STM 15-15. **B.** Glide polar graph in 4 models of STM 15-15 compared to modern soaring birds.



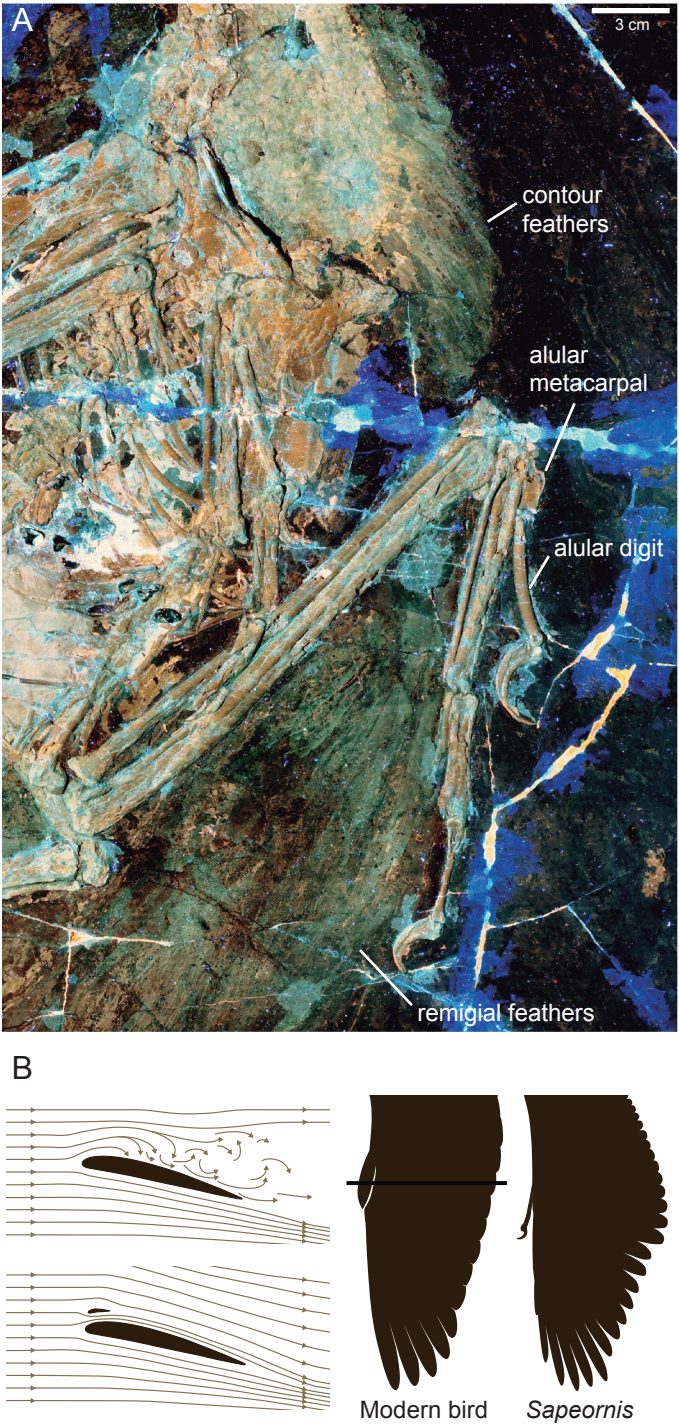


FIG. 4. **A.** LSF image of hand and feathers of STM 15-15. **B.** Effect of alula delaying stall, and wing silhouettes of an avian (crown bird) and *Sapeornis*.

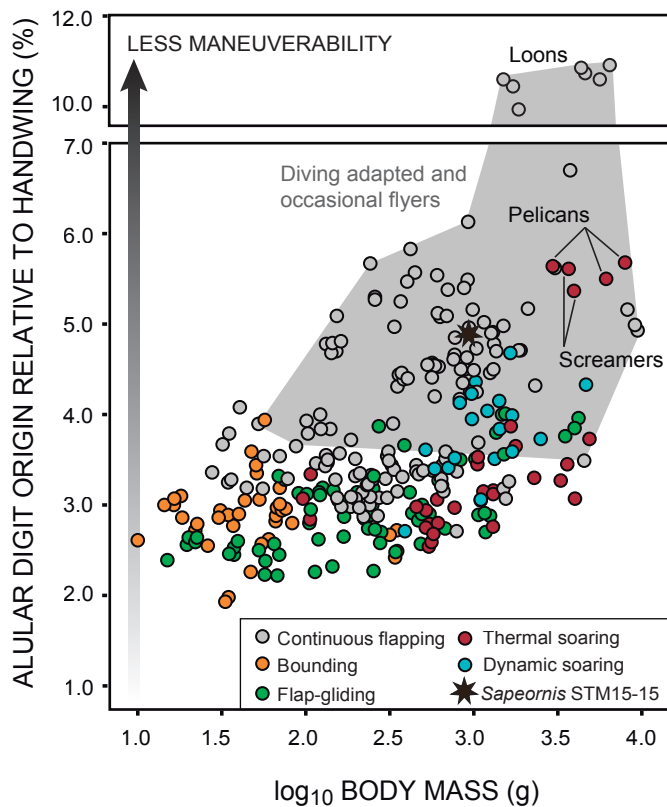


FIG. 5. Scatter graph of alular digit position against  $M_b$ , compared with modern bird morphospace.

the area of the wings (Taylor and Thomas, 2014). The congruence between the aerodynamic models 1 and 2 (fig. 3) validates the assumptions made in Serrano and Chiappe's (2017) previous assessment of the flight performance of *Sapeornis*. However, such assumptions should probably be validated on a case-by-case basis, especially given the often large morphological differences between modern and early-diverging bird species as well as the availability of direct soft-tissue data using imaging methods like LSF. In order to minimize this issue, we delimited the flight reconstruction of STM 15-15 using minimum and maximum values (models 3 and 4) based on  $C_{Db}$  observed in modern birds (Pennycuik, 2008; Hedenström and Liechti, 2001). Finally, the negative power margin during flapping flight and the gliding pattern obtained in the four models (fig. 3) corroborate the hypothesis that

*Sapeornis* had thermal soaring capabilities, as proposed by Serrano and Chiappe (2017).

Furthermore, we argue that the alular digit, albeit lacking a true alula as shown by LSF (fig. 4A), was a functional precursor of the true alula (Meseguer et al., 2012), thus acting as an anti-stall device that increased control at low speeds (fig. 4B). Our study documents a distalward location of the alular digit of *Sapeornis* (fig. 5), which implies that a lesser portion of the proximal handwing was under the influence of this flap. Such position of the alular digit (and functional flap) suggests that the maneuverability of *Sapeornis* might have been weak when compared with that of modern soaring birds of similar size. Lastly, from a paleoecological perspective, these results indicate that if *Sapeornis* was capable of perching, as suggested by the bird's pedal anatomy (Glen and Bennett, 2007;



Chiappe and Meng, 2016), its limited capacity to maneuver would have hindered its abilities to land on a perch.

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